

# 1.011 Project Evaluation: Comparing Costs & Benefits

Carl D. Martland

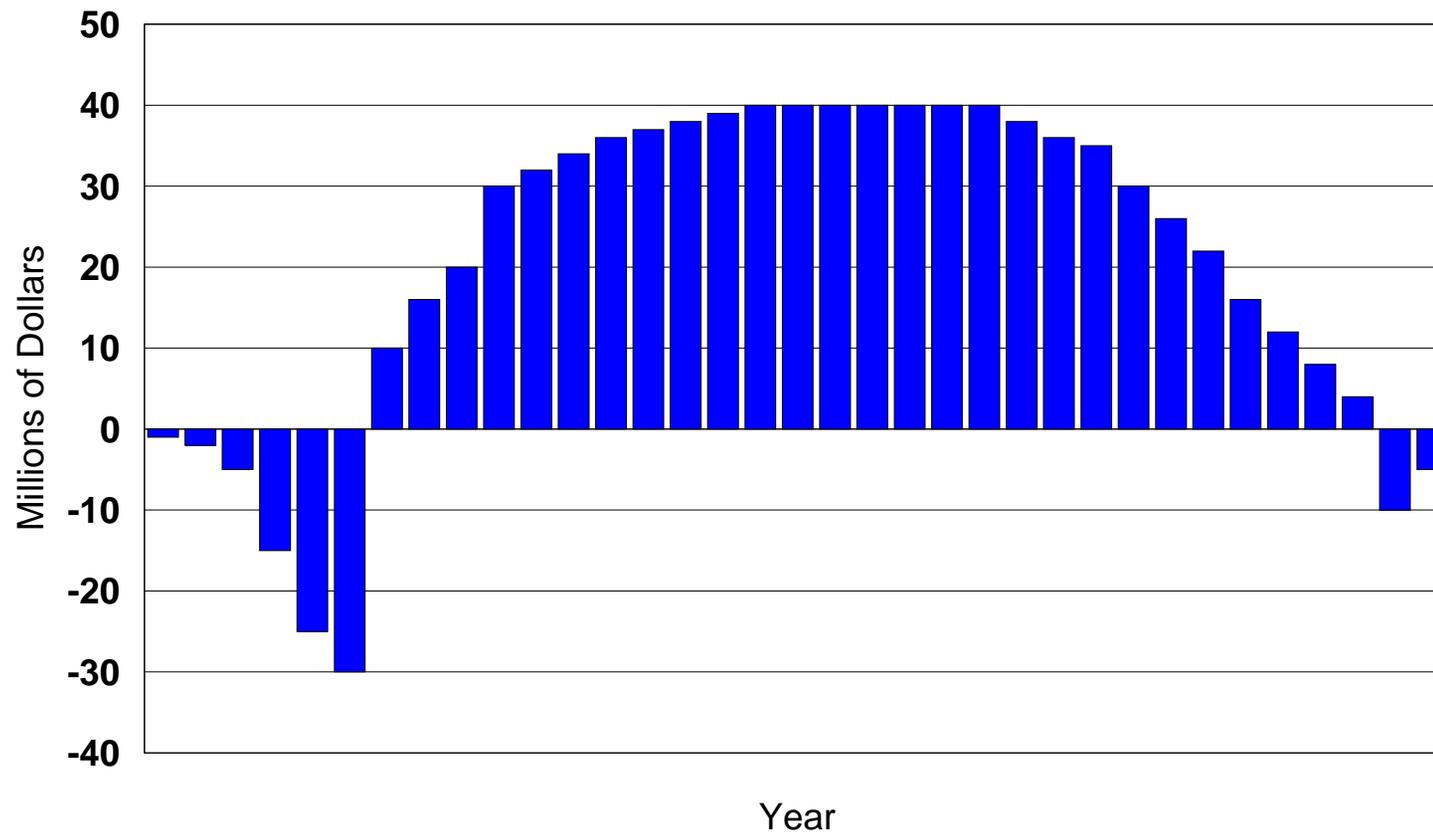
- Basic Question:
  - ▶ Are the future benefits large enough to justify the costs of the project?
- Present, Future, and Annual Worth
- Internal & External Rates of Return



# How Do We Justify a Project?

- Is this project worthwhile?
  - ▶ *Are the benefits greater than the costs?*
    - ***Are MY benefits greater than MY costs?***
- Is this the best way to achieve these benefits (either engineering & institutional options)?
  - ▶ *Can similar benefits be achieved more efficiently by some other approach?*
- Is this the best place to allocate resources?
  - ▶ *Do other projects have greater payoff?*
  - ▶ *Are other types of benefits more important?*

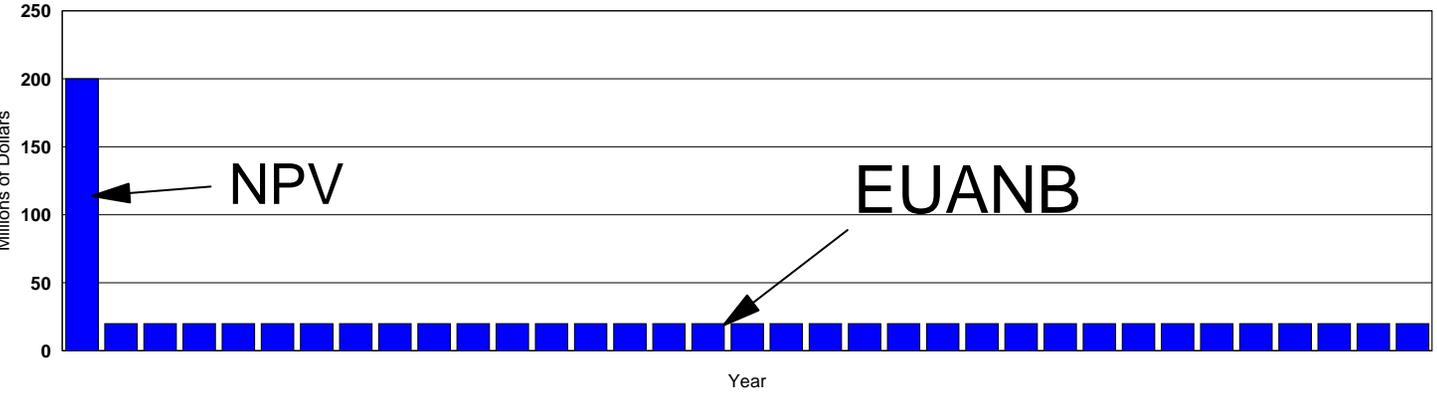
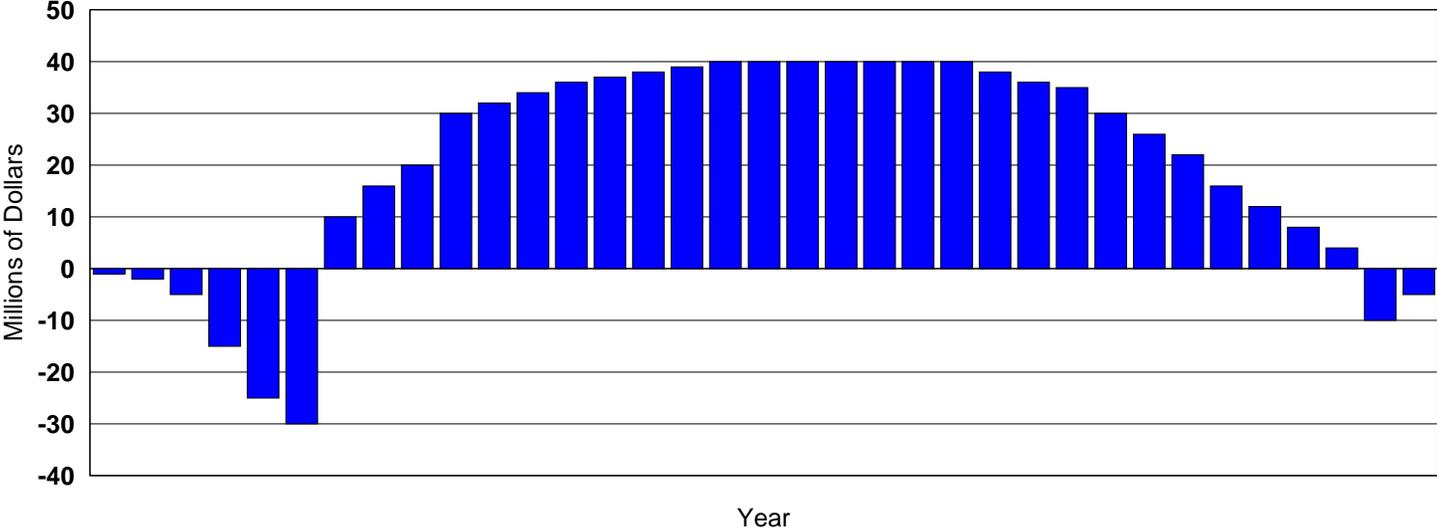
# Cash Flow of a Typical CEE Project



# Evaluating a Time Stream of Monetary Costs & Benefits

- Key concepts:
  - ▶ Time value of money
  - ▶ Risk vs. required return
  - ▶ Present Worth (= Net Present Value)
  - ▶ Equivalence (for PW, FW, and AW)
  - ▶ Project Life

# Cash Flows, NPV, and Equivalent Uniform Annual Net Benefits

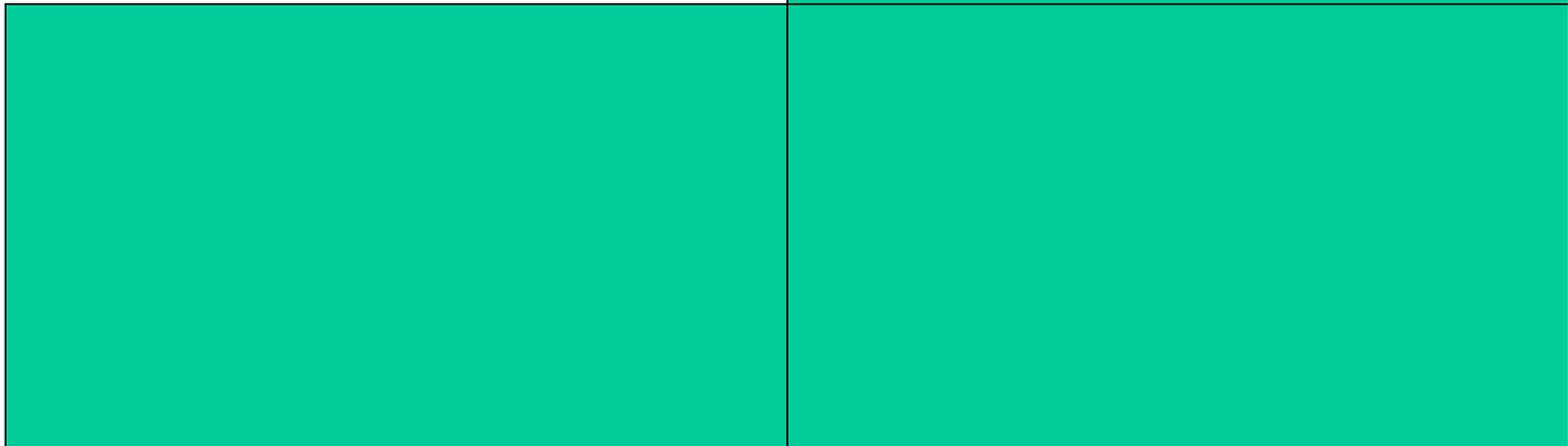
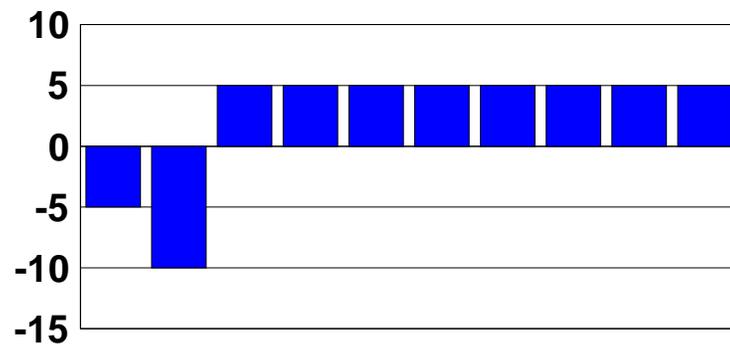


# Importance of the Project Life

- Projects need to be evaluated over a reasonable project life (and the economic life will be shorter than physical life)
  - ▶ However, your choice of a project life should NOT determine the outcome of the analysis (if it does, you must show sensitivity of the results to project life)
- Because of discounting, the "out years" do not add much to the NPV, so a 20 to 50 year life is usually sufficient for analysis
  - ▶ The proper assumption is that the very long term effects will be positive or neutral - NOT that we can live it up now and let our children and grandchildren worry about the future!
- Risks increase with time
  - ▶ So we don't want to be dependent on long-term benefits to recover our investment.

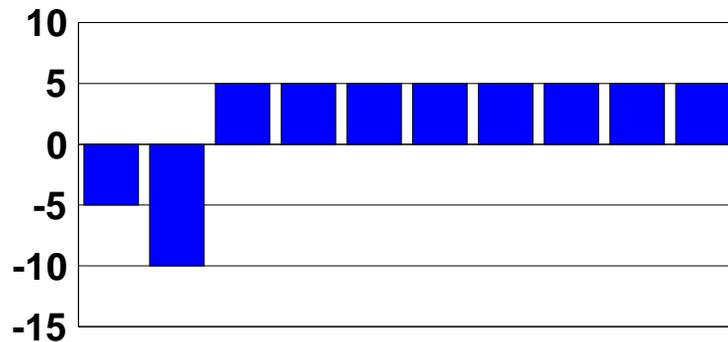
# Choice of a Project Life Should NOT Determine the Outcome of Your Analysis!

A. Net Cash Flows Over a 10-Year Life

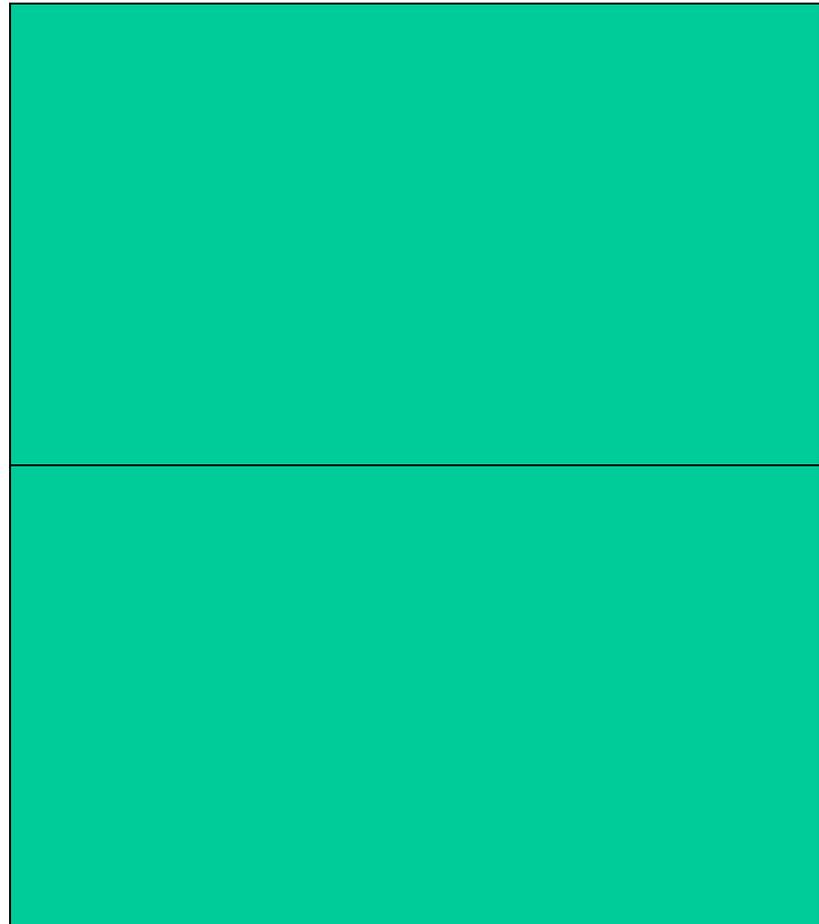
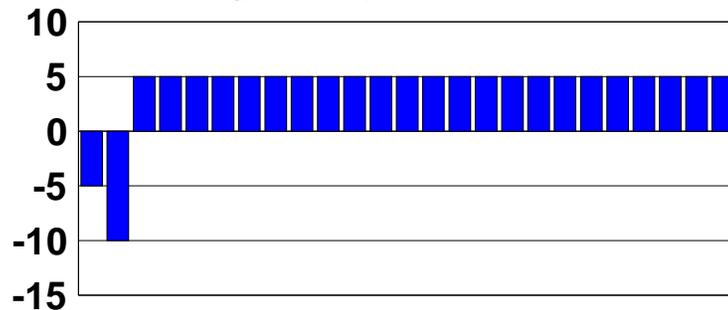


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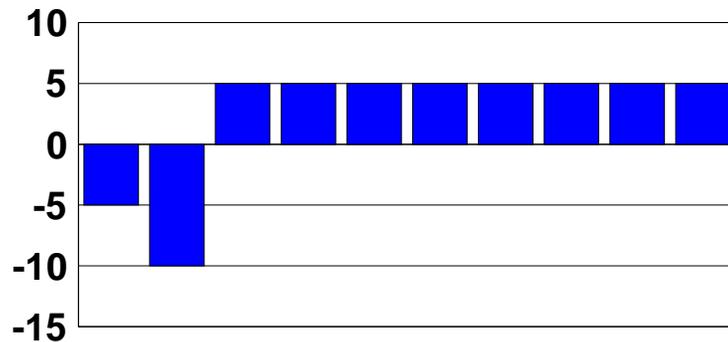


B. Net Cash Flows Over 25 Years  
(Assuming Steady State After Year 10)

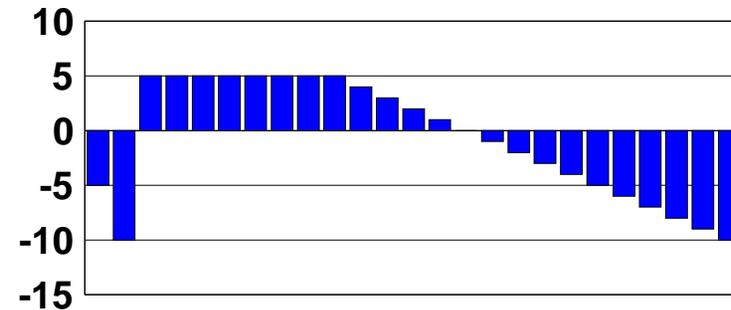


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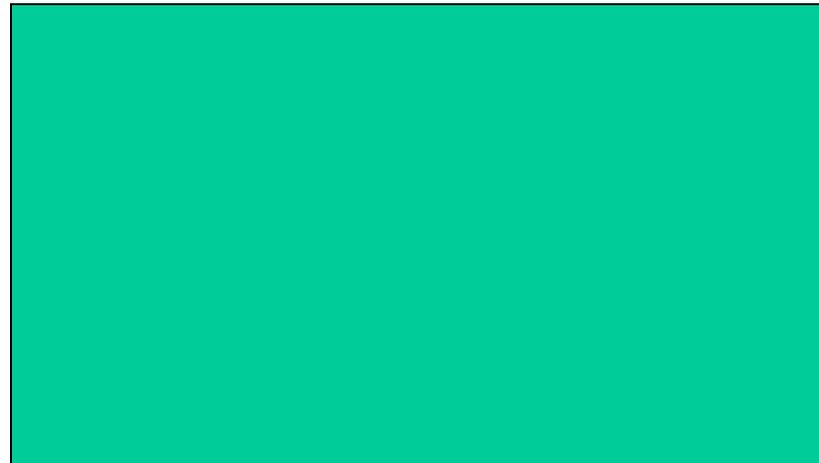
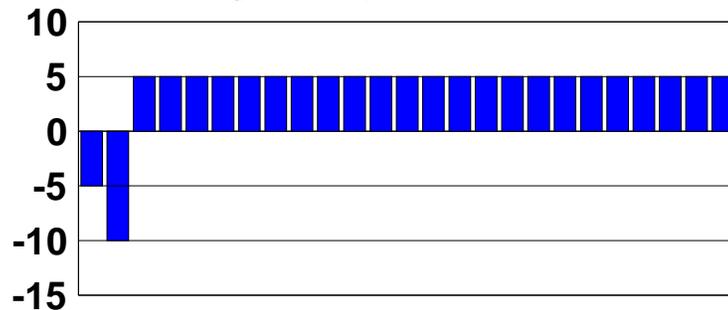
A. Net Cash Flows Over a 10-Year Life



C. Cash Flows Over 25 Years  
(Increasing Competition & Maintenance)

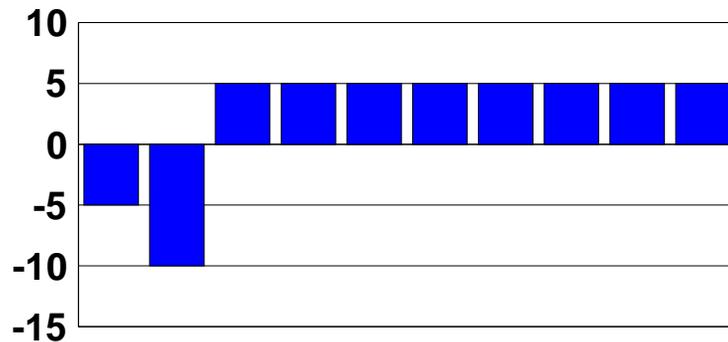


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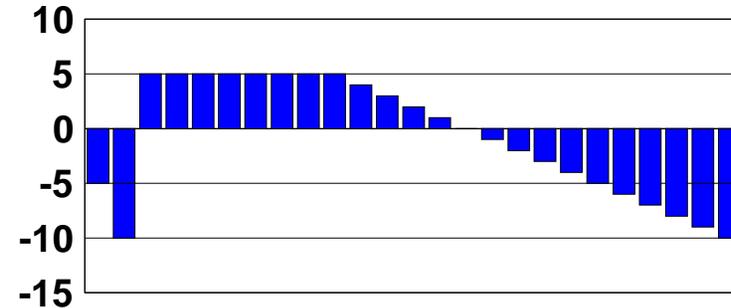


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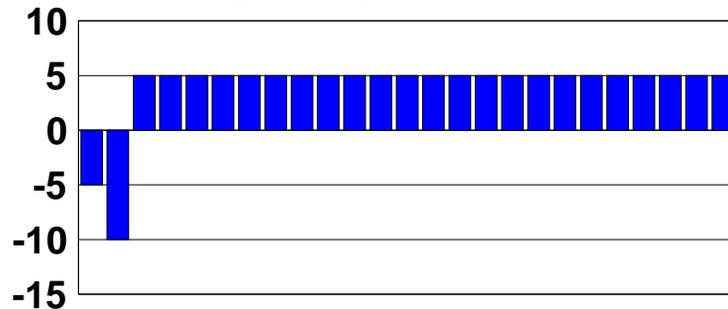
A. Net Cash Flows Over a 10-Year Life



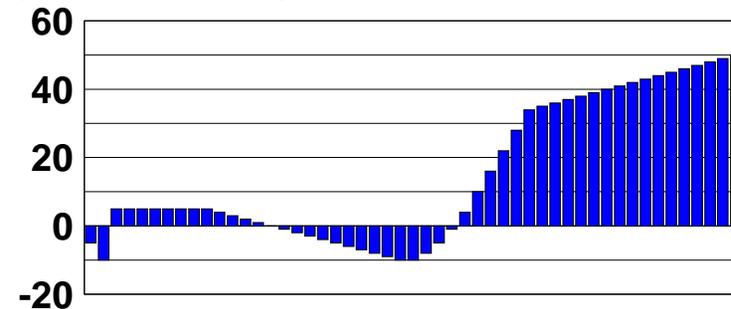
C. Cash Flows Over 25 Years  
(Increasing Competition & Maintenance)



B. Net Cash Flows Over 25 Years  
(Assuming Steady State After Year 10)



D. Net Cash Flows Over 50 Years  
(Rehab and Expansion in Prime Location)



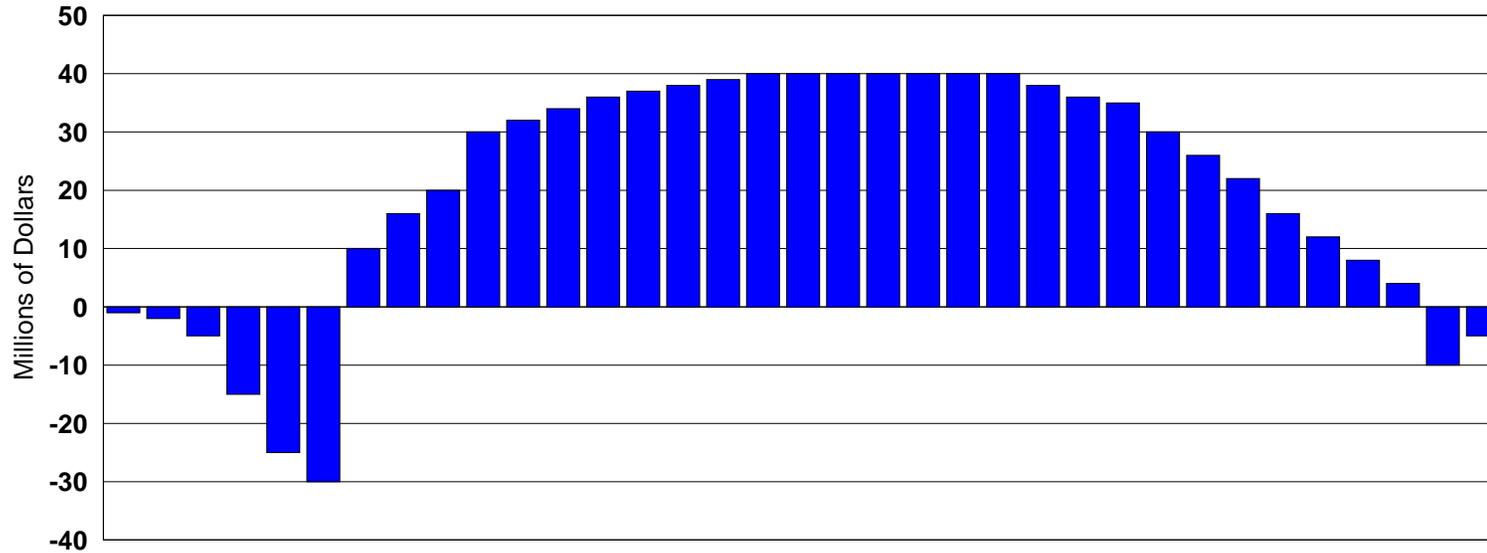
# Meaning of NPV

- $NPV > 0$ , using a discount rate of  $i\%$ 
  - ▶ This project is better than making an investment at  $i\%$  per year for the life of the project
  - ▶ This project is worth further consideration
- $NPV < 0$ , using a discount rate of  $i\%$ 
  - ▶ This project does not provide enough financial benefits to justify investment, since alternative investments are available that will earn  $i\%$  (that is what is meant by "Minimum Acceptable Rate of Return" )
  - ▶ The project will need additional, possibly non-cash benefits to be justified

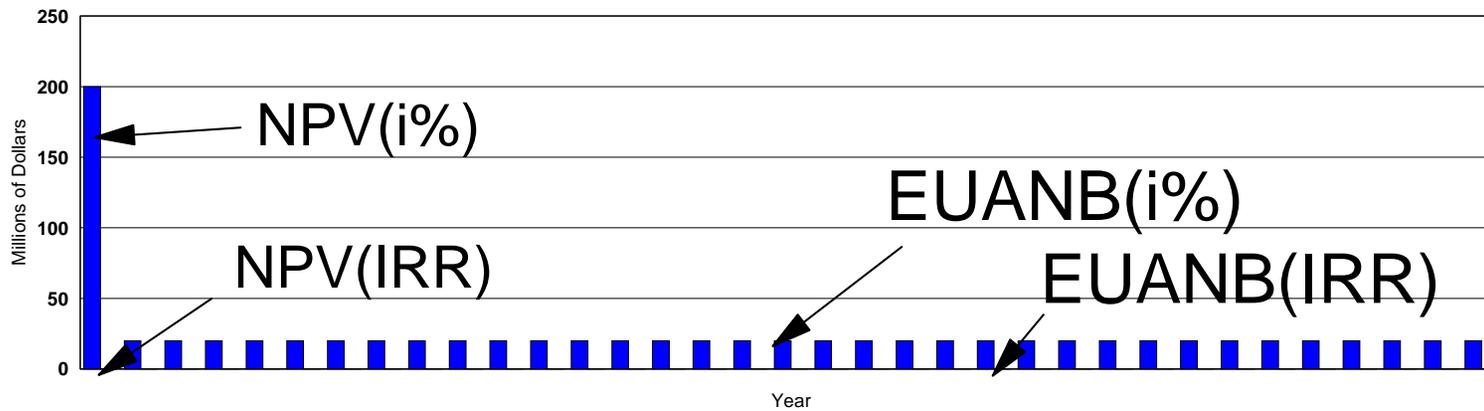
# Other Ways to Evaluate Cash Flows

- Benefit/Cost Ratios
  - ▶  $\text{NPV}(\text{Benefits})/\text{NPV}(\text{Costs})$
  - ▶ Commonly used in public policy analyses
    - Required in order to ensure that benefits (by SOME measure at least!) are greater than costs
    - A political, not a methodological statement!
- Internal and External Rates of Return (IRR and ERR)
  - ▶ Very common in private sector, but there may be problems with IRR (which can be fixed by using ERR)
- Payback Period
  - ▶ How many years to recoup my investment? (A rather unsatisfactory approach that may be useful for quick assessment of some projects)

# Calculating the Internal Rate of Return



Choose discount rate such that the NPV = 0



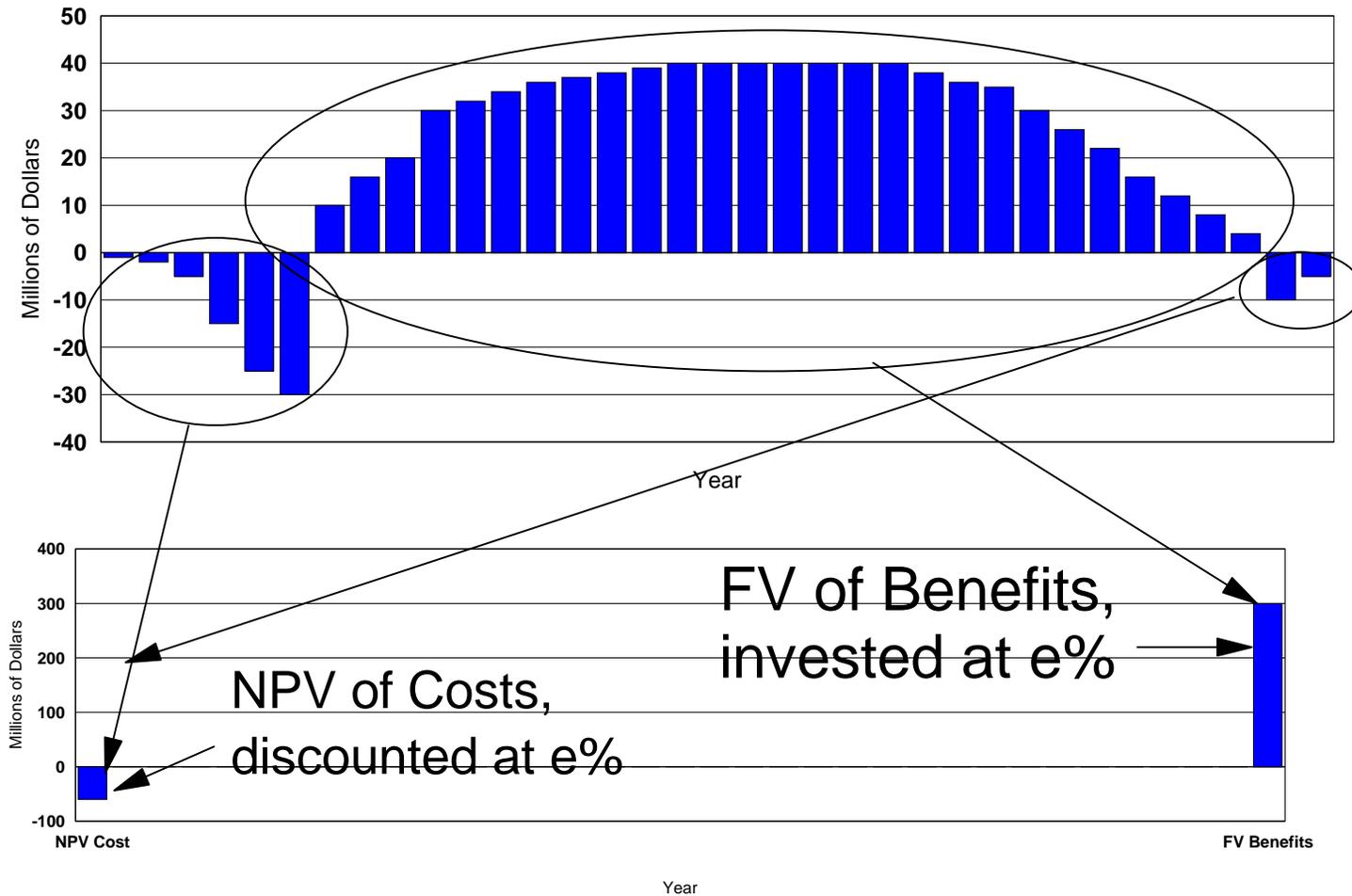
# Problems With the Internal Rate of Return

- If the cash flows switch signs more than once, there could be two or more IRR for which  $NPV(IRR) = 0$
- This method assumes that all intermediate cash flows can be discounted/reinvested at the IRR
  - ▶ This is unrealistic when the IRR is very high
- The private sector uses this method very commonly despite these problems

# A Better Approach: The External Rate of Return

- Use a different discount rate (called the "External Rate of Return") to
  - ▶ Discount all expenses to time 0
  - ▶ Reinvest all benefits for the remaining time in the project life
- Then compare the NPV of the costs and the Future Value of the benefits
  - ▶ The external rate of return is the discount rate s.t. the NPV of the costs is equivalent to the FV of the benefits

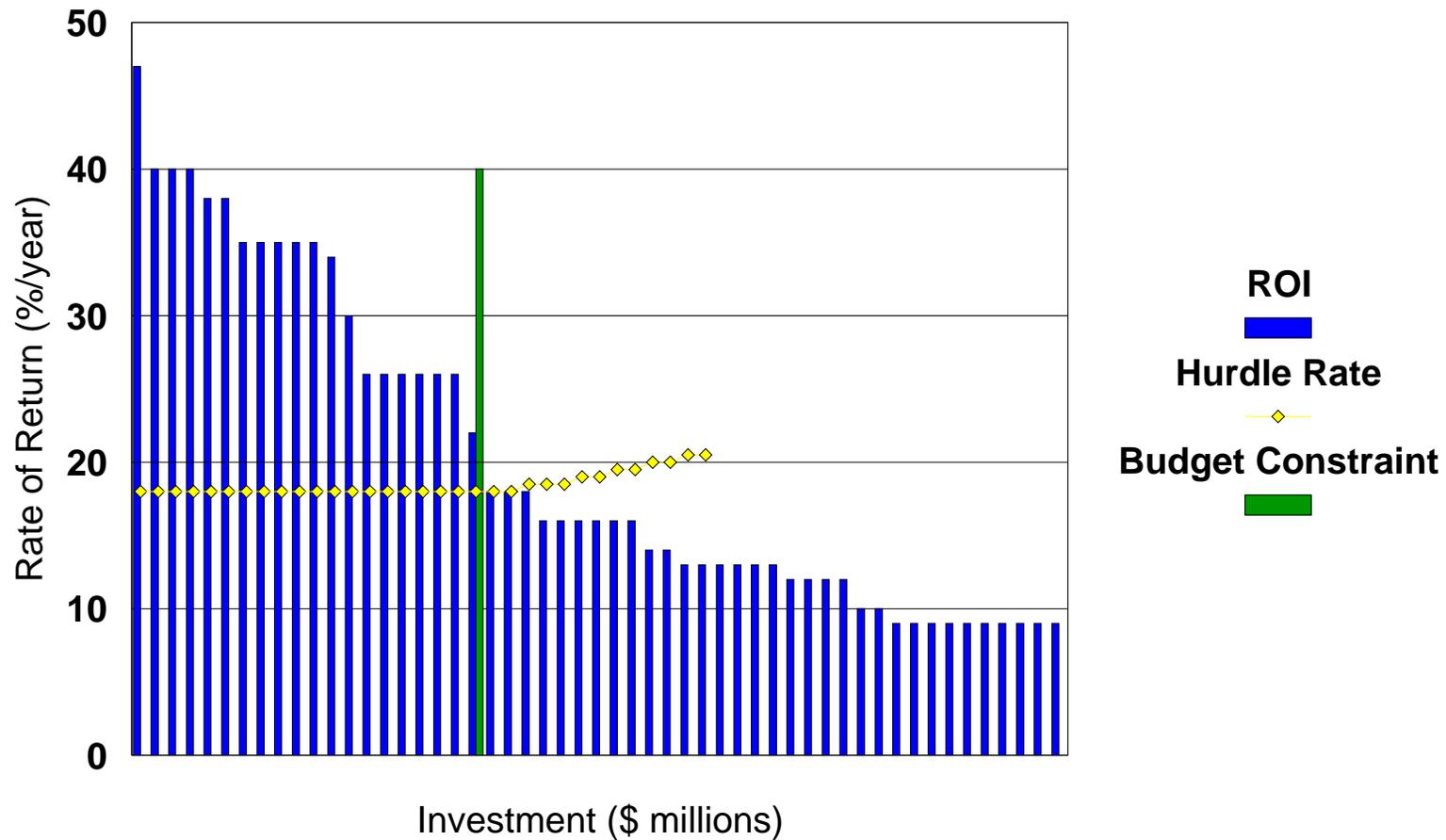
# Calculating the External Rate of Return



# Can We Justify this Project Against Competing Projects?

- In principle, any project with  $NPV > 0$  is worth pursuing.
- In practice, capital budgets are limited, so that choices must be made:
  - ▶ What set of projects gives the greatest benefits from using the available resources?
- Common approach in private sector: Hurdle rate of return:
  - ▶ Rank independent projects by rate of return (typically IRR, but should be ERR):
  - ▶ Choose projects (or sets of projects) with highest return subject to a budget constraint

# Selecting Projects Based Upon a Hurdle Rate of Return



# Ranking Projects

- Using PW, AW or FW will give the same ranking for independent projects or independent sets of projects.
- Maximizing PW does seem to be the right objective.
- QUESTIONS:
  - ▶ Will IRR rank projects the same way as PW, AW or FW?
  - ▶ Will IRR select the wrong projects?

# Mutually Exclusive Projects

- “Sometimes you have to finally decide, make up your mind, let the other one ride”
- You want the best project – and some projects with apparently acceptable returns really are not acceptable
- You need to be very careful when using IRR to rank projects

# An Example of Inconsistent Rankings

(E.E. Section 5.4.2.1)

	A	B	A-B
Capital Investment	-\$60,000	-\$73,000	-\$13,000
Revenue - Expense	\$22,000/yr	\$26,225/yr	\$4,225/yr
PW	\$9,738	<b>\$10,131</b>	
IRR	<b>17.3%</b>	16.3%	
Project life	4 years	4 years	

# How Do We Resolve the Inconsistency?

Is the smaller investment acceptable? Yes,  $PW > 0$

Is the INCREMENTAL investment of \$13,000 justified by the incremental return?

\$4,225 extra for four years, at MARR = 10%

$$PW = \$4225 * (P/A, 10\%, 4) = \$4,225 * 3.169$$

$$= \$13,393 > \$13,000$$

The PW of the INCREMENTAL investment is positive, so the incremental investment is better, even though the IRR is lower!

# Example 1: Lesson

- Of all the options with  $PW > 0$ , let the base case be the option with the lowest capital cost
- Consider the next largest investment if the incremental return on the incremental investment is greater than the MARR
  - ▶ This means that the IRR on the incremental investment exceeds the MARR
- Recommend the largest investment where the incremental investment is justifiable

## Example 2: More Options

(Amounts in \$1000s)

		Invest	Net Income
Park	Parking Lot	\$200	\$22
B1	1 Story Building	4,000	\$600
B2	2 Story Building	5,500	\$720
B3	3 Story Building	7,500	\$960

# Example 2: Incremental Analysis

(Amounts in \$1000s)

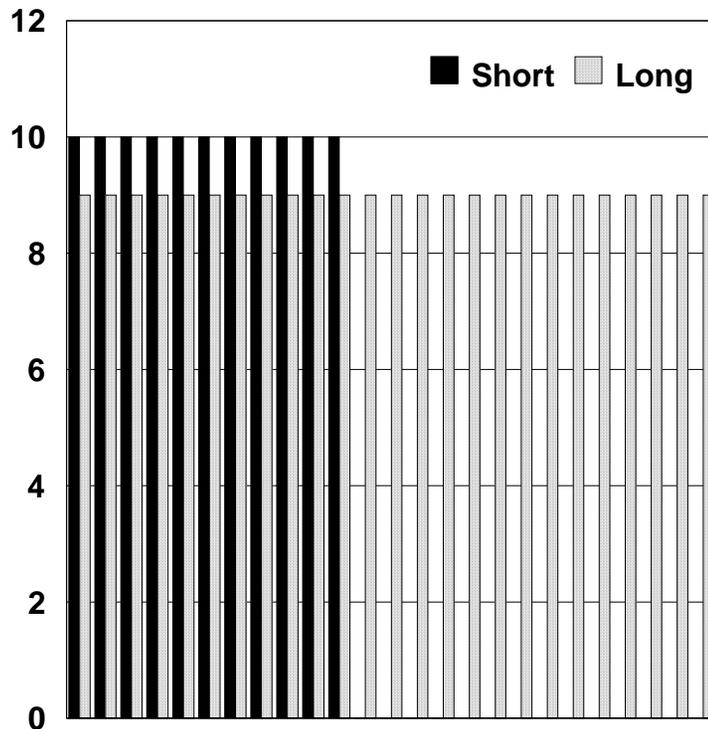
	B1-P	B2-B1	B3-B1
$\Delta K$	-\$3,800	-\$1,550	-\$3,500
$\Delta \text{Inc}$	\$578	\$120	\$360
$\Delta \text{IRR}$	15.2%	7.7%	10.3%
	OK	NDG!	OK

# If Project Lives Are Different

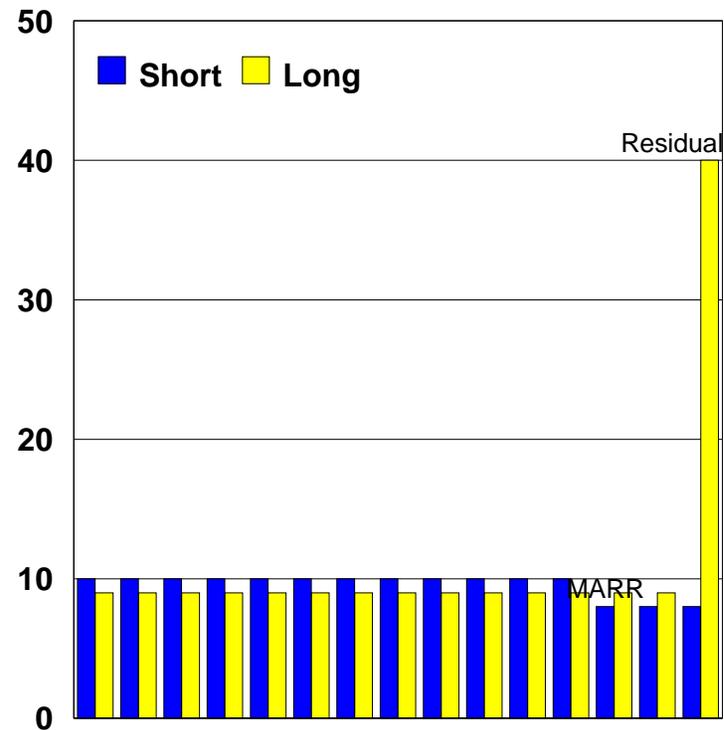
- Use a longer life that is an integral multiple of both lives, e.g. use a 20 year life to compare projects of 4, 5, or 10 years duration
- Estimate a residual value for the project with a longer life and use the life of the shorter-lived project
- Use a sufficiently long life that the differences will be negligible
- Use the AW method (and assume that you would replace your project with one that is at least that good)
- Use common sense and do sensitivity analysis if you are in doubt! There is NO right method!

# Comparing Projects With Unequal Lives Using MARR & Residual Value

Comparison of Short & Long-L



Comparison Over 15 Year Proj



# Summary

- The equivalent worth methods are computationally less cumbersome to use and to understand
- Both the equivalent worth and the IRR/ERR methods will give the correct choice if used properly
- IRR/ERR methods will give the **WRONG** choice if a manager insists on the highest return rather than ensuring that the incremental IRR is greater than the MARR

# Questionable Assumptions

- We know the MARR
  - ▶ *In principle we should, but this is a little fuzzy!*
- We know the limit for capital expenditures
  - ▶ *The limit is always negotiated - who has the power in the corporation? who can convince the board to go ahead? who can convince people to buy bonds?*
- We have an ordered list of ALL feasible projects, none of which are mutually exclusive
  - ▶ *Highly unlikely! No one who has seriously considered design assumes they can EVER know ALL of the alternatives, many of which are mutually exclusive!*
- Decision-makers use PW, AW, or FW methods
  - ▶ *In fact, they prefer using the Internal Rate of Return!*

# Are There Alternatives For Achieving the Objectives of this Project?

- The NPV analysis only shows that a project can be justified relative to the discount rate that is used
- There may be other projects that are even better for achieving the same objectives:
  - ▶ Better materials & technologies to build the same facility
  - ▶ Different design for a structure to serve the same purpose
  - ▶ Different location for a similar structure
  - ▶ Different scale (larger or smaller)
- In general, you cannot prove that your design is the best, you can only defend and refine (or abandon) your design in response to other options

# Broader Economic Issues

- Prices of resources may not reflect their true costs
  - ▶ Local rather than world rates for energy costs
  - ▶ Natural resources priced at extraction cost rather than at market cost
  - ▶ Opportunity cost of land may be omitted (build the highway through the park)
  - ▶ Government may require use of excess labor as a public policy
- Generational equity
  - ▶ Discounting of future costs and benefits may lead to long-term decline in the environment
  - ▶ "Worry about today and the future will take care of itself"

# Broader Economic Issues (Continued)

- Distributional Equity
  - ▶ Costs and benefits will be unevenly distributed
  - ▶ If total benefits exceed total costs, there is at least a possibility of compensating the losers
  - ▶ Pareto optimality - some are better off and none are worse off (after compensation)
  - ▶ "No one is hurt" (a very strong constraint on development)\
- Regional Economic Impact
  - ▶ Multiplier effect of project expenditures on the local economy
  - ▶ Use of local labor & resources
- Non-financial Externalities
  - ▶ Many impacts - both positive and negative - may be left out of the cash flow analysis
  - ▶ Environmental impacts & need for remediation

## **Broader Economic Issues - Conclusions**

- For any large project, there will be additional costs & benefits that must be considered in addition to the cash flows directly related to the project
- Some of these costs and benefits cannot readily be reduced to monetary measures
- Distribution of costs & benefits will be a concern
- In some cases, the non-quantifiable items will be the most important items to consider

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